

5/13/08

14.129

I

◦ Legros-Newman: "Competing for Ownership"

◦ Two types of production units: 1, 2

◦ Each with risk neutral manager and a continuum of assets

◦ Continuum of production units: type 1: $i \in I = [0, 1]$

type 2: $j \in J = [0, n]$

◦ relatively scarce unit

◦ Standalone production gives 0 surplus

◦ "Cooperation" between one type 1 and one type 2 gives positive surplus

◦ Surplus depends on "planning decisions" in production, which are never contractible, but "who is allowed to plan" is contractible.

◦ related to individual assets

◦ planning decisions will involve private costs (effort)

◦ Each manager i has cash $l_1(i) \geq 0$ if type 1

j has cash $l_2(j)$ if type 2

◦ wlog, $l_1(i), l_2(j)$ increasing

◦ Assets in type 1 unit: $k \in [0, 1]$

type 2 unit: $k \in [1, 2]$

◦ Their contribution to profits are proportional to planning decisions $q(k) \in [0, 1]$

◦ Firm will succeed (implies revenue $R > 0$) w/prob $p(q)$

fail (implies zero revenue) w/prob $1 - p(q)$

◦ $p(q) = \gamma \int_0^2 q(k) dk$

◦ productivity $A = \gamma R$

5/13/08

14.129

2

- private cost $c(q(k)) = \begin{cases} \frac{(q(k))^2}{2} & \text{for } k \in [0, 1] \\ 0 & \text{for } k \in [1, 2] \end{cases}$ for type 1 manager
 - $c(q(k)) = \begin{cases} 0 & \text{for } k \in [0, 1] \\ \frac{(q(k))^2}{2} & \text{for } k \in [1, 2] \end{cases}$ for type 2 manager
- There is an ex post moral hazard here.

$$C_1(q) = \int_0^1 c(q(k)) dk$$

$$C_2(q) = \int_1^2 c(q(k)) dk$$

- Contracts: decision q is never contractible
- right to decide on q is contractible.

→ (ω, t)

type 1 "controls" assets in $[0, 1-\omega]$ → transfer

type 2 "controls" assets in $[1-\omega, 2]$ $-1 < \omega < 1$ } $\omega = 0 \Rightarrow$ nonintegration

(*) why can't a third party control all the assets?

$$u_1(\omega, t) = \max_{\substack{q(k) \in [0, 1] \\ k \in [0, 1-\omega]}} \frac{A}{2} \int_0^2 q(k) dk - \frac{1}{2} \int_0^1 q(k)^2 dk - t$$

$$u_2(\omega, t) = \max_{\substack{q(k) \in [0, 1] \\ k \in [1-\omega, 2]}} \frac{A}{2} \int_0^2 q(k) dk - \frac{1}{2} \int_1^2 q(k)^2 dk + t$$

$$\text{Assume } \omega > 0 \Rightarrow q(k) = \begin{cases} \frac{A}{2} & \text{for man 1 for } k \in [0, 1-\omega] \\ \frac{A}{2} & \text{for man 2 for } k \in [1, 2] \\ 1 & \text{for man 1 for } k \in [1-\omega, 1] \end{cases}$$

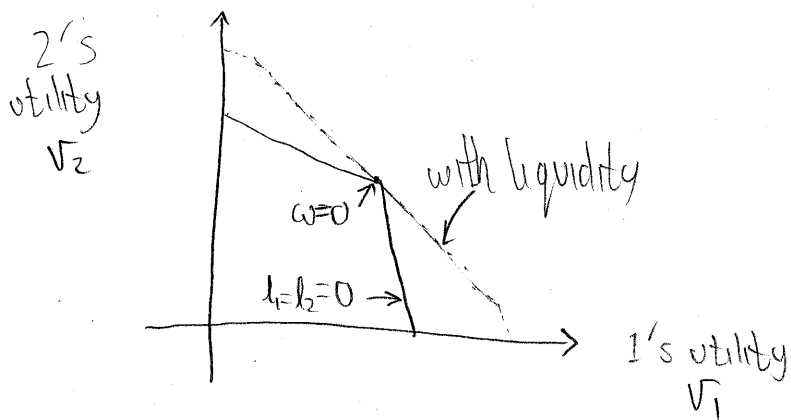
Payoffs: $u_1(\omega, t) = \frac{3A^2}{8} - \omega(2-A)^2/8 - t$

$$u_2(\omega, t) = \frac{3A^2}{8} + \omega(2-A)/4 + t$$

5/13/08

14.129

3



Determine type 1's willingness to pay:

$$\max_{(\omega, t)} u_2(\omega, t)$$

(ω, t)

must be feasible

$$\text{s.t. } u_1(\omega, 0) \geq t$$

$$t \in [0, l_1]$$

$$\text{solution: } (\omega, t) = \begin{cases} (0, \frac{3}{8} A^2) & \text{if } l_1 \geq \frac{3}{8} A^2 \\ \left(\frac{3A^2 - l_1}{(2-A)^2}, l_1 \right) & \text{if } l_1 < \frac{3}{8} A^2 \end{cases}$$

Type 2 surplus

