

$$y_1 = \beta y_2 + \varepsilon$$

$$y_2 = Z\pi + v$$

\Rightarrow run first stage and get \hat{v}

Run regression:

$$y_1 = \beta y_2 + \alpha \hat{v} + \eta$$

$\alpha = 0$? Control function approach

What about the nonlinear case?

Petrin:

Problems with BLP:

- It is complicated and might not give the right answer
- The inversion requires the idiosyncratic term to enter in linearly. Suppose it is: $\gamma_{\beta^1} \xi_j^1 + \gamma_{\beta^2} \xi_j^2$

Reduced form for prices:

$$P = P(\underbrace{Z_1}_{\text{dmd shifts (product characteristics)}}, \underbrace{Z_2}_{\text{cost shifts (instruments)}}, \underbrace{\xi_j}_{\text{unobserved heterogeneity}})$$

(1)

- Find some proxy $\tilde{\xi}$ obtained from inverting (1).
- This approach combines BLP with nonlinear IV
- Need conditions for this inversion to exist.

1 product case: Newey and Imbens (2003)

- can get this $\tilde{\xi}$ right away

Multiple product case is difficult

Petrin: For the additively separable case,

$$P_{mj} = f_j(Z_m) + g_j(S_m), \quad f_j(Z_m) \text{ an unknown function.}$$

$$= E[P_j | Z_m] + g_j(S_m) \quad (??)$$

$$\tilde{S}_m = (g_1(S_m), \dots, g_j(S_m))$$

◦ stack the residuals from each market

◦ use $\tilde{S}_j = \underbrace{\Lambda^{-1}}_{\text{scalar}} \tilde{S}_m$ as a proxy in:

$$\pi P_j S_j + \pi P_j^2 \tilde{S}_j \quad \text{equation}$$

◦ why is this okay to do?