

1a) $x_i^* \in S_i(p, w_i(p))$ $y_j^* \in \eta_j(p)$
 $px_i^* = w_i(p)$ $py_j^* = \sup pY_j$
 $x_i > x_i^* \Rightarrow px_i > px_i^*$ $py_j^* \geq py_j$

$\sum px_i - \sum py_j = p[\sum x_i - \sum y_j] > p[\sum x_i^* - \sum y_j^*] = p \cdot \omega$
 $\Rightarrow [(x_i), (y_j)]$ is not feasible since $x - y > \omega$.

$\sum w_i(p) = w(p) = p \cdot \omega + \sum_j \pi_j(p)$



PTE } alternative arguments for efficiency of competitive markets.
 Coase Theorem }

Without competition, there will be waste.
 ↳ Rubinstein's bargaining model is a possible counterexample.

$k \quad 1 \quad 2 \quad 3 \quad \dots \quad T \quad \dots$
 $S = (I, II, I, II, \dots)$
 size of pie: $1, \frac{1}{s}, \frac{1}{s^2}, \frac{1}{s^3}, \dots$

["Nash program" - Can we take cooperative equilibria (efficient) and support them as NE in a non-cooperative game?]

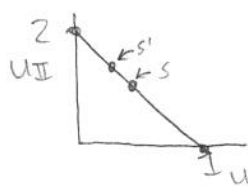
$(u_I(s), u_{II}(s))$ - SG-PNE payoffs

$u_I(s) + u_{II}(s) = 1$

$\Rightarrow 1/2 + 1/2 = 1$

$s' = (I, II, II, I, II, II, I, II, II, \dots)$

$u_I(s') + u_{II}(s') = 1$



can trace out entire horizon by varying the S vectors. This is an analogy of the 2nd theorem of welfare economics.

Want to criticize this as "game-taking behavior."

$MP_i^+(s) \quad i \in \{I, II\}$
 $= \begin{cases} u_i(s) - u_i(s_{-i}, s_i \neq i) & \text{if } s_i = i \\ 0 & \text{otherwise} \end{cases}$

Claim: $u_i(s) = \sum_{t=1}^{\infty} MP_i^+(s)$.

Games of length T :

$$S = (I, II, \dots, I \vee II)$$

$$t = 1, 2, \dots, T$$

Externality $v_i(z_i, z_j), j \neq i$

Public good $v_i(z)$ (will have the free-rider problem)

Pecuniary vs real externalities

↳ the kind that individuals create is a problem

With respect to individual behavior, pecuniary and real externalities are "the same."

There is a beautiful pricing duality with respect to public goods.

Both externalities and public goods have notions of "local" and "global."