

2002 MT Q2

$$v(1,2,3) = 1$$

$$v(i,j) = \alpha = 1 \geq 2/3 \quad \forall i,j$$

$$v(i) = 0$$

$$v(\emptyset) = 0$$

convexification arises from the indivisibility of labor (fractional matching also convexifies)

LP

$$\sum_{T \in \mathcal{I}} v(T) x(T)$$

$$\text{st } \sum_{T \in \mathcal{I}} x(T) \leq 1$$

in assign. model:

$$(P) \max \sum_{b,s} v(b,s) x(b,s)$$

$$C: \sum_i \sum_z x_i(z) \leq 0 \quad \leftarrow \text{commodity constraint}$$

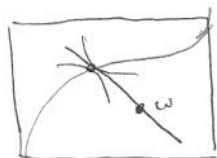
$$I: \sum_z x_i(z) \leq r_i \quad \leftarrow \text{individual constraint}$$

$$(D) v(b,s) \leq q_b + q_s$$

$$x(b,s) > 0 \Rightarrow v(b,s) = q_b + q_s$$

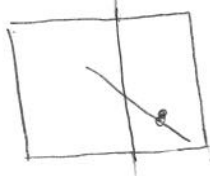
2004 MT Q4

non-QL



Price-taking can be viewed as a mechanism in a

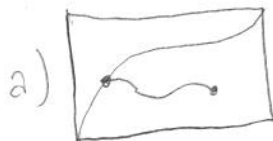
QL



small economy

In a large economy, it is "almost" Nash to "play" price-taking!

begin with  $w$  at  $t=0$ . Do not consume until  $t=T$   
 Suppose I have the following mechanism: Can be creative



b) The only possible endpoints are when  $z = \bar{z}$

2004 F comp Q5

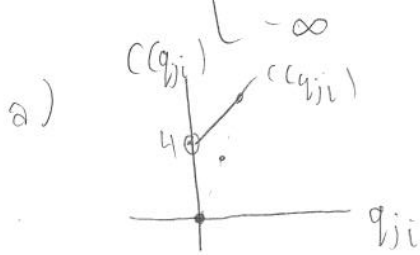
It is widely thought that perfect competition drives toward linear pricing.

$j = 1, 2$   
 $i = 1, 2.$

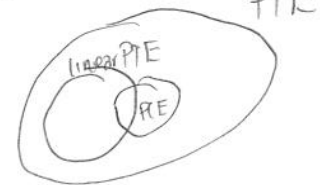
$$c(q_{ji}) = \begin{cases} 0 & q_{ji} = 0 \\ q_{ji} + 4 & q_{ji} > 0 \end{cases}$$

$q_{ji}$  = quant  $j$  delivers to  $i$ .

$$v(q_i) = \begin{cases} 10q_i & 0 \leq q_i \leq 1 \\ -\infty & \text{else} \end{cases}$$



supplied  
 $q_{ji} = 0$   
 but  $q_{ji}$  demanded = 1



b)

$$V_I(0) = 10 + 10 - (4+1) - (4+1) = 10$$

$$V_{II}(1) = 10 - (4+1) = 5$$

$$V_{II}(2) = 10 + 10 - (4+1) - (4+1) = 10$$

$$MP_j = 0$$

$$MP_i = 5$$

$\sum MP_i + \sum MP_j = 10 \Rightarrow$  Full appropriation.  
 Yes, unless  $n=1$ .

c) Entry fee and user fee. In this case,  
 $\frac{4}{4}$                        $\frac{1}{1}$

$$\pi_j = 4 + 1 - (4 + 1) = 0 = MP_j.$$

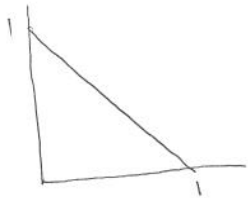
d)

$$c(q_j) = \begin{cases} 4 & q_j = 0 \\ q_j + 4 & q_j > 0 \end{cases}$$



convexifying effect  
 price-taking equilibrium sort of exists in the limit.

2003 Fall Q6



$c \in [0, 1]$  no fixed costs.  
 $MC=AC=c$ ,  $c$  unknown.  
 $D=1-p$

Story: monopoly reports  $c'$ . Government implements a

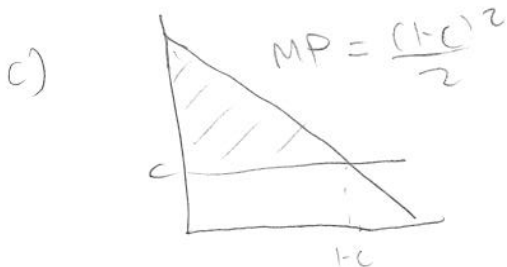
a)  $1 - c' = q(c')$

b)  $\hat{\pi}_M(c'; c) = q(c')c' - q(c')c$

True  $c$  such that it is incentive compatible?

$\pi_M(c'; c) = (1 - c')c' - (1 - c')c$

$\frac{\partial \pi}{\partial c'} = 0 \Rightarrow 1 - 2c' + c = 0 \Rightarrow c' = \frac{1+c}{2}$   
 $c' = c$  iff  $c = 1$



Report  $c$  and I will give you  $\frac{(1-c)^2}{2} + c(1-c)$

$\hat{\pi} = \frac{(1-c')^2}{2} + c'(1-c') - (1-c')c = \frac{1-2c'+c'^2}{2} + c' - c'^2 - c + cc'$

$\frac{\partial \hat{\pi}}{\partial c'} = 0 \Rightarrow -1 + c' + 1 - 2c' + c = 0 \Rightarrow c' = c \forall c \in [0, 1]$

