

- Read everything up to §3A (official)
  - Angrist-Levy-Schlosser } Tuesday (unofficial)
  - Becker
  - Angrist JLE '96 (Palestinian Labor) } Thursday
- Gelbach AER 2003

$$h_{is} = \alpha_0 + \underbrace{K_{is}^1}_{\text{in kindergarten?}} \beta + \sum_{is} \gamma + \alpha_s + \epsilon_{is}$$

hours for mother

◦ why not OLS?

- selection ( $K_{is}^1 = 1 \Rightarrow$  different types of mothers)
- endogenous  $K_{is}^1$  (strategic enrollment)

◦ use quarter of birth:  $Q_{is}$

$$h_{is} = \alpha_0 + Q_{is} \pi + \dots ?$$

From 2SLS:  $\hat{\beta} = 2.7$

Omitted variables: # children and age of mother

Differences in differences

Spse interested in effects of immigration on native job market.

Natural experiment: city lets in a lot of workers

Assume:  $E[Y | c, t] = \beta_t + \gamma_c$

unemployment rate  $\nearrow$  city time

$$E[Y | c, t, T=1] = \beta_t + \gamma_c + \delta$$

treatment?

$$= E[Y | c, t, T=0] + \delta$$

Spse we look at:

$$E[Y | c, t, T=1] - E[Y | c, t', T=0] = \Delta \beta_t + \delta$$

not zero, so this clearly doesn't identify  $\delta$

$$E[Y | c, t, T=1] - E[Y | c', t, T=0] = \Delta \gamma_c + \delta$$

similarly

Thus, we look at:

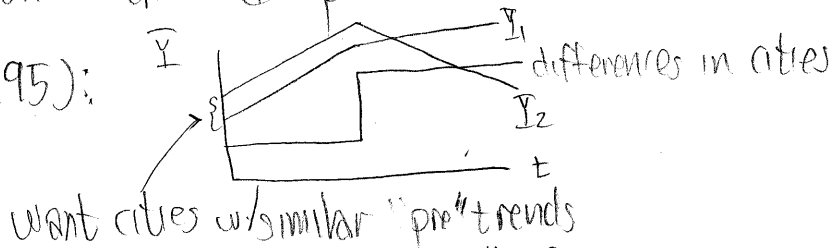
$$[E[Y | c, t, T=1] - E[Y | c, t', T=1]]$$

$$- [E[Y | c, t, T=0] - E[Y | c, t', T=0]] = \Delta \beta_t - \Delta \beta_t + \delta = \delta$$

◦ Policy endogeneity is a potential problem. We usually ignore this.

◦ Interactions are a problem as well

Eissa (1995):



◦ want things to look at this.

◦ interaction terms matter

Card 1990

◦ Mariel Boat Lift (Cuban immigration into Miami)

◦ Finds  $\delta = 0$ .

Standard errors were handled incorrectly in the past  
Bertrand-Duflo-Mullainathan (BDM)

$$y_{its} = \sum x_{its} \beta + \epsilon_{its}$$

$$\text{Var}(\hat{\beta}_{OLS}) = (X'X)^{-1} X' \underbrace{\text{Var}(\varepsilon)}_{\Omega} X (X'X)^{-1}$$

iid:  $\Omega = \begin{bmatrix} \sigma^2 & 0 \\ 0 & \sigma^2 \end{bmatrix} = \sigma^2 I_n$  (sphericity)

Heteroskedasticity:  $\Omega = \begin{bmatrix} \sigma_1^2 & 0 \\ 0 & \sigma_n^2 \end{bmatrix} = E[\varepsilon\varepsilon']$

$$\widehat{\text{Var}}(\hat{\beta}_{OLS}) = (X'X)^{-1} \hat{E}[(X'\varepsilon)(X'\varepsilon)'] (X'X)^{-1}$$

$$\rightarrow \hat{E}[\varepsilon_i^2 X_i X_i'] \leftarrow \frac{1}{n} \sum_{i=1}^n \varepsilon_i^2 X_i X_i'$$

BDM:  $\Omega = \begin{bmatrix} V & 0 \\ 0 & V \end{bmatrix}$ , where  $V = \begin{bmatrix} \sigma_c^2 + \sigma_v^2 & \sigma_c^2 & \dots & \sigma_c^2 \\ \sigma_c^2 & \sigma_c^2 + \sigma_v^2 & & \\ & & \dots & \\ & & & \sigma_c^2 \end{bmatrix}$

Moulton correction: can estimate  $\hat{\beta}$ :  $V = \begin{bmatrix} 1 & \hat{\beta} \\ & \vdots \\ & \hat{\beta} \end{bmatrix}$

restrictive, since it assumes a pretty restrictive error structure.

also  $\rightarrow \frac{\sigma^2 (X'X)^{-1} X' \Omega X (X'X)^{-1}}{\sigma^2 (X'X)^{-1}} = 1 + \left[ \frac{\text{var}(m_i)}{\bar{m}} + \bar{m} - 1 \right] \rho_X \rho$

where  $\rho_X = \text{corr}(X_{1s}, X_{js})$

$$\begin{aligned} y_{ts} &= X_{ts}' \beta + \varepsilon_{ts} \\ \varepsilon_{ts} &= \rho \varepsilon_{t-1, s} + \nu_t \end{aligned} \quad \left. \vphantom{\begin{aligned} y_{ts} &= X_{ts}' \beta + \varepsilon_{ts} \\ \varepsilon_{ts} &= \rho \varepsilon_{t-1, s} + \nu_t \end{aligned}} \right\} \text{serial correlation}$$

Two problems: • Moulton problem  
• serial correlation

Solution: clustering the standard errors

$$\widehat{\text{Var}}(\hat{\beta}) = (\bar{X}'\bar{X})^{-1} \left( \sum_{s=1}^S \bar{X}_s' \hat{\epsilon}_s \hat{\epsilon}_s' \bar{X}_s \right) (\bar{X}'\bar{X})^{-1}$$

◦ need lots of states