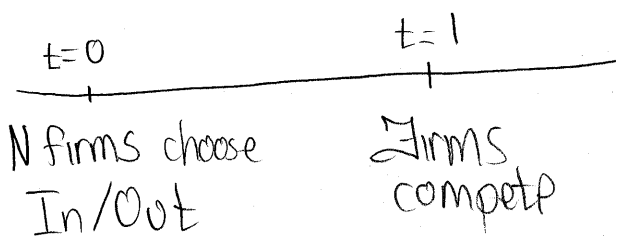
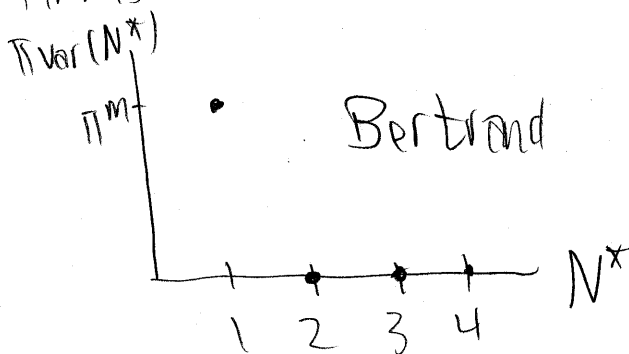
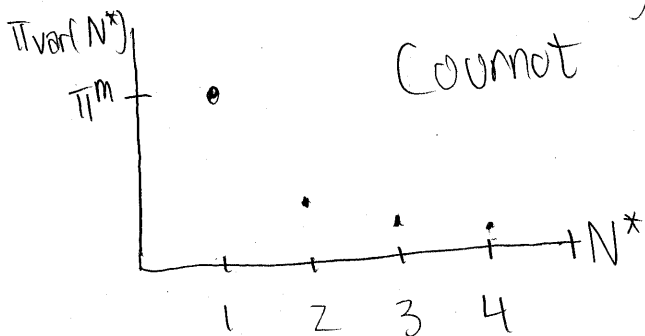


# Entry



Suppose  $N$  is very large, so some firms will choose not to enter

- Homogeneous good
  - Demand  $Q(p)$  downward sloping
- Sunk cost  $K$  of entry
- Cost  $C(Q)$  of producing  $Q$  units
- Assume competition at  $t=1$  produces:
  - $p^*(N^*)$
  - $Q^*(N^*)$  - output for individual firm
  - $\pi_{var}^*(N^*) = Q^*(N^*)P^*(N^*) - C(Q^*(N^*))$
  - variable profit
  - where  $N^* = *$  entering firms



In a pure strategy SPE, it must be that

$$\pi_{var}^*(N^*) \geq K \geq \pi_{var}^*(N^* + 1)$$

- sometimes, people assume  $\pi_{var}^*(N^*) = K$ , where  $N^*$  need not be an equilibrium
- Not highly recommended

- In a mixed strategy SPE, generically at least two firms mix
  - $\tilde{N}$  - the realized  $N^*$  is a random variable
  - Sometimes,  $\pi_{\text{var}}^*(\tilde{N}) > K$ , and sometimes  $\pi_{\text{var}}^*(\tilde{N}) < K$
  - Each firm is indifferent between entering and not entering.

### Observations:

1] Lower fixed costs  $\Rightarrow$  more firms in equilibrium.

2] If  $\pi_{\text{var}}^*(N^*) > 0 \quad \forall N^*$ , then  $N^* \rightarrow +\infty$  as  $K \rightarrow 0$

3] In this model, profits are a rounding error, not directly related to toughness of competition.

### Notation change

### Welfare effects of entry

◦ Suppose  $N$ , not  $N^*$ , is the # firms that enter.

$$W_N = \sum_{i=1}^N \pi_{\text{var}}^*(N) + CS(N) - NK$$

welfare with  $N$  firms in mkt

◦ usually talk about 2nd-best welfare

◦ optimal  $N$  given  $p^*(N), q^*(N)$

◦ obviously the optimal  $N$  would be 1 if we could ensure MC pricing.

$$W_{N+1} = \sum_{i=1}^{N+1} \pi_{\text{var}}^*(N+1) + (S(N+1) - (N+1)K)$$

$$\Delta W = W_{N+1} - W_N$$

$$= \left[ \pi_{\text{var}}^*(N+1) - K \right] + \sum_{i=1}^N \underbrace{(\pi_{\text{var}}^*(N+1) - \pi_{\text{var}}^*(N))}_{\text{change in } \pi \text{ of incumbent firms} \equiv A} + (S(N+1) - S(N))$$

### Reasons for departure from optimality

- 1] Business stealing effect. Entering firm will not take into account  $A < 0$ 
  - Negative externality ( $N$  will be too high)
- 2] Firms also ignore  $(S(N+1) - S(N)) > 0$ 
  - Positive externality. ( $N$  will be too low)

### 3] Discreteness

Proposition: Consider homogeneous good model with no discreteness issues. That is  $N^*$  satisfies

$$\pi_{\text{var}}^*(N^*) = K. \text{ If}$$

$$1] \frac{\partial}{\partial N} N Q^*(N) > 0$$

aggregate output increases

$$2] \frac{\partial}{\partial N} Q^*(N) < 0$$

individual output decreases

$$3] p^*(N) - C'(Q^*(N)) > 0 \quad \forall N$$

Then,  $N^* \geq N^{\text{SB}}$ , where  $N^{\text{SB}}$  maximizes

$$W_N. \quad (\text{ie } N^{\text{SB}} = \arg \max_N W_N)$$

Proof:  $N^{SB} = \operatorname{argmax}_N \underbrace{\int_0^{Nq^*(N)} p(s) ds}_{\text{gross consumer surplus}} - \underbrace{NcQ^*(N) - NK}_{\text{total costs}}$

$$(N): 0 = W'(N^{SB})$$

$$= P(N^{SB} Q^*(N^{SB})) [Q^*(N^{SB}) + N(Q^*)'(N^{SB})]$$

$$- [cQ^*(N^{SB}) + Nc'(Q^*(N^{SB}))](Q^*)'(N^{SB}) - K$$

$$= \underbrace{P(N^{SB} Q^*(N^{SB})) Q^*(N^{SB}) - cQ^*(N^{SB})}_{\pi_{\text{var}}^*(N^{SB})} (Q^*)'(N^{SB}) - K$$

$$+ \underbrace{N^{SB} (Q^*)'(N^{SB})}_{(-)} \left[ \underbrace{P(N^{SB} Q^*(N^{SB})) - c'(Q^*(N^{SB}))}_{(+)} \right]$$

$$\Rightarrow \pi_{\text{var}}^*(N^{SB}) - K > 0$$

Since  $N^*$  is s.t.  $\pi_{\text{var}}^*(N^*) - K = 0$ , assuming a single crossing property (ie  $\pi_{\text{var}}^*(N)$  is decreasing in  $N$ ), then  $N^* \geq N^{SB}$ .

Remark: Too many firms due to business stealing.

◦ Can easily have  $N^* < N^{SB}$  with discreteness taken into account.

◦ Suppose  $D(p) = 1 - p$ ,  $c = 0$ , Bertrand competition

$$\circ N=1 \Rightarrow p = \frac{1}{2}, \pi = \frac{1}{4}, CS = \frac{1}{8} \Rightarrow W_1 = \frac{3}{8} - K$$

$$\circ N=2 \Rightarrow p = 0, \pi_1 = \pi_2 = 0, CS = \frac{1}{2} \Rightarrow W_2 = \frac{1}{2} - 2K$$

• For  $K \in (0, \frac{1}{8})$ , 2 firms is better than 1, but  $\pi_2 - K < 0$ , so we will only have one firm.

$$\Rightarrow N^{SB} = 2, N^* = 1 \Rightarrow N^* < N^{SB}$$

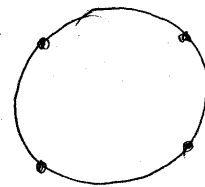
## Entry with Horizontal Differentiation

Consider competition on a circle

• circle circumference 1

• values  $v - t/d$

• mass  $m$  of consumers



$t=0$	$t=1$
In/out decision	Competition on a circle

$$\circ p^*(N) = c + \frac{t}{N}$$

$$\circ \pi_{var}^*(N) = \frac{M}{N} \cdot \frac{t}{N} = K \quad \text{in equilibrium}$$

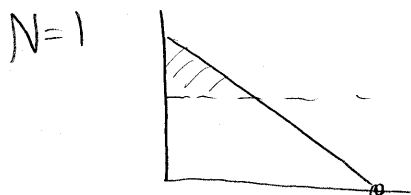
$$\Rightarrow N^* = \sqrt{\frac{Mt}{K}}$$

Note

1]  $N^* \rightarrow +\infty$  as  $K \rightarrow 0$

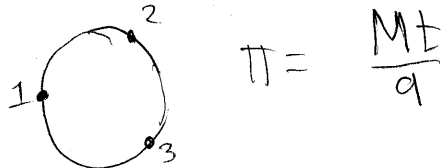
2] Larger  $M \Rightarrow$  Larger firms

3] Extra CS effect relative to homogeneous good model.

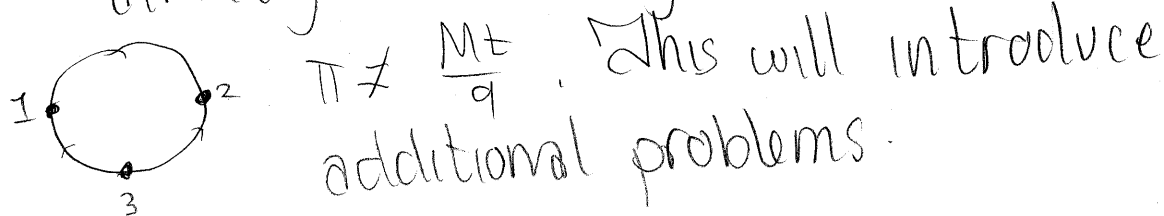


4] If firms are allowed to choose location, get greater scope for rounding errors.

◦  $N=3$  and uniformly located, we get



◦  $N=3$ , but if firms 1 and 2 were already uniformly located,



Entry with vertical differentiation

◦ Consumers have value  $\theta v_i - p_i, \theta \sim U[a, b]$

◦ Firms choose location  $v_i \in [\underline{v}, \bar{v}]$

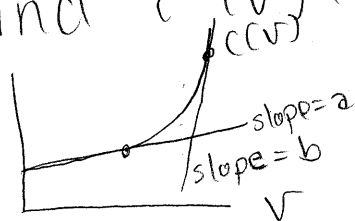
- Fixed cost  $K$ , marginal cost  $c(v)$  (constant)
- fixed cost same no matter what the quality. Marginal cost depends on quality.

Case 1: Suppose  $c'(v) < a \forall v$  or  $c'(v) > b \forall v$ .  
Then, only a finite number of firms enter for any given  $K$ . (i.e.  $\exists \bar{N}$  s.t.  $N^*(K) < \bar{N} \forall K$ )

Intuition: Suppose  $c'(v) < a \forall v$ . Then  $\bar{v}$  is the efficient product quality.

- If  $N \rightarrow \infty$  as  $K \rightarrow 0$ , then  $p(v) \rightarrow c(v)$ .  
at  $c(v)$ , only  $\bar{v}$  is purchased. This implies  $\pi^* = 0$  for many firms.

Case 2: Suppose  $c'(v) < a$  for some  $v \in [\underline{v}, \bar{v}]$   
and  $c'(v) > b$  for some  $v \in [\underline{v}, \bar{v}]$ .



Then  $\exists$  equilibria in which  $N^* \rightarrow +\infty$  as  $K \rightarrow 0$ .

- all firms choose  $v$ 's with  $c'(v) \in [a, b]$

Next time: ◦ Jovanovich paper

- Empirical papers (Barry, Woldfogel, and others)